

ACTIVITY

Area Of Parallelogram

Objective

To show that the area of a parallelogram is equal to the product of its base and corresponding height by using paper cutting and pasting.

Material Required

Glazed papers, pencil, a pair of scissors, glue stick.

Theory

1. Construction of parallelogram by paper folding.
2. Area of rectangle = length \times breadth
3. Area of parallelogram = base \times corresponding height.

Procedure

1. Draw a parallelogram by paper folding using colored glazed paper and name it ABCD.
2. Cut the parallelogram with the help of scissors.
3. In the parallelogram, draw a perpendicular from a vertex D to its opposite side AB of the parallelogram ABCD by paper folding.
4. We will get a crease along with DE. Dark the color in $\triangle ADE$ [fig (i)]. Now cut it along DE. We will get two pieces, one triangle named as AED and the other one a trapezium named $E'D'CB$ as shown in fig. (ii).

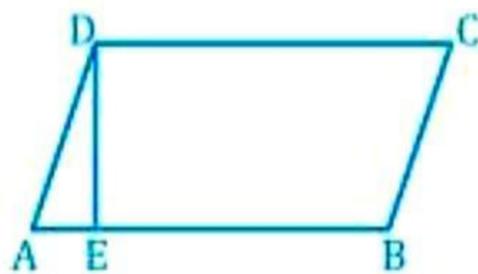


Fig. (i)

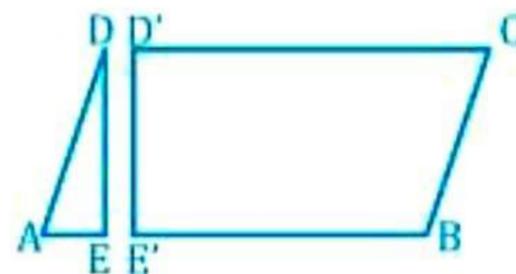


Fig. (ii)

5. Paste this triangular piece AED on the other side of trapezium such that its side AD coincides with BC [fig. (iii)].

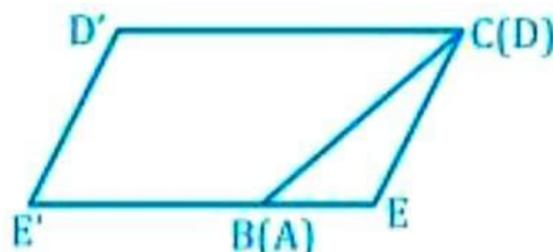
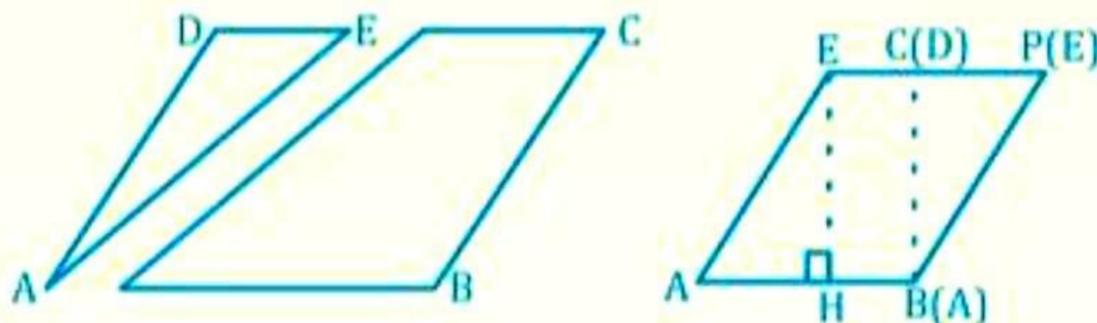


Fig. (iii)

6. After pasting, we get a rectangle $E'ECD'$ with length as $E'B + BE = E'E = D'C = AB$ and breadth as $E'D' = EC$.



Observation

We observe that new figure D'E'EC is a rectangle.

$$\begin{aligned}
 \text{Area of parallelogram } ABCD &= \text{Area of rectangle } E'ECD' \\
 &= \text{length} \times \text{breadth} \\
 &= E'E \times D'E' \\
 &= AB \times DE
 \end{aligned}$$

Hence, Area of parallelogram = Base \times Height

Result

It is verified that the area of a parallelogram is equal to the product of its base and corresponding height by the paper cutting and pasting method.

Learning Outcome

We can draw a perpendicular from different vertices on opposite sides of a parallelogram and verify that the area of the parallelogram is the product of base and height.

Area of a parallelogram with the same base and the same height are identical. This leads to a famous theorem:

“Parallelogram between the same parallel lines and on the same base are equal in area.”

Activity Time

Verify the area of a parallelogram is equal to the product of its base and corresponding height in which perpendicular falls outside the base of the parallelogram.

Viva Voce

Q1. How does a diagonal of a parallelogram form two triangles of equal area?

Ans: A diagonal of a parallelogram divides it into two triangles of equal area.

Q2. In a parallelogram if $AB = 4 \text{ cm}$, $BC = 6 \text{ cm}$, $CD = 8 \text{ cm}$ and $AD = 10 \text{ cm}$ then find perimeter of parallelogram.

Ans: $P = 28 \text{ cm}$.

Q3. If one side of a parallelogram is 10 cm and its area is 60 cm^2 . Find the corresponding altitude.

Ans: Side of the parallelogram (base) = 10 cm

$$\text{Area of the parallelogram} = 60 \text{ cm}^2$$

$$\text{Now, base} \times \text{altitude} = 60 \text{ cm}^2$$

$$\Rightarrow \text{altitude} = \frac{60 \text{ cm}^2}{10 \text{ cm}} = 6 \text{ cm}$$

Q4. If the base of a parallelogram is 5 cm and the corresponding altitude is 3 cm . Find the area of the parallelogram.

Ans: Base of the parallelogram = 5 cm
 Corresponding altitude of the parallelogram = 3 cm
 Area of the parallelogram = $5 \times 3 \text{ cm}^2 = 15 \text{ cm}^2$.

Q5. What is the area of a triangle?

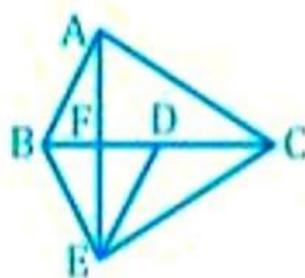
Ans: Area of a triangle = $\frac{1}{2} \times \text{base} \times \text{height}$.

Q6. Define an altitude of a quadrilateral.

Ans: An altitude of a quadrilateral is a perpendicular line segment joining a vertex of the quadrilateral to the opposite side

Multiple Choice Questions

Q 1. In the figure, ABC and BDE are two equilateral triangles such that D is the mid-point of BC. If AB intersects DE in F, then we have



(a) Area ($\triangle BDE$) = $\frac{1}{4}$ area ($\triangle ABC$)

(b) Area ($\triangle BDE$) = $\frac{1}{2}$ area ($\triangle BAF$)

(c) Area ($\triangle BEF$) = 2 area ($\triangle FED$)

(d) Area ($\triangle FED$) = $\frac{1}{4}$ area ($\triangle AFC$)

Q 2. If Diagonals AC and BD of a quadrilateral ABCD intersect at O in such a way that ar($\triangle AOD$) = ar($\triangle BOC$). Then ABCD is a:

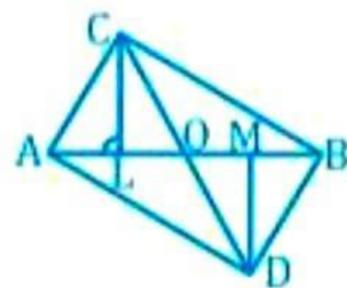
(a) Parallelogram

(b) Rectangle

(c) Square

(d) Trapezium

Q 3. If ar(parallelogram ABCD) = 25 cm^2 and ar($\triangle BCD$) = $x \text{ cm}^2$, then the value of x is:



(a) 25 cm^2

(b) 50 cm^2

(c) 12.5 cm

(d) 12.5 cm^2

Q 4. Given, a triangle ABC and E is the mid-point of median AD of $\triangle ABC$. If ar($\triangle BED$) = 20 cm^2 , then ar($\triangle ABC$) is:

(a) 10 cm^2

(b) 5 cm^2

(c) 60 cm^2

(d) 80 cm^2

Q 5. Measure of one angle of a parallelogram is $\frac{2}{3}$ of its measure of the adjacent angle. Measure of the smaller angle of the parallelogram is:

(a) 54°

(b) 72°

(c) 81°

(d) 108°

ANSWER KEY

1.(a) 2.(d) 3.(a) 4.(c) 5.(b)